

Berechne:

$$a) \frac{\sqrt{500}}{\sqrt{25} \cdot \sqrt{10}} = \sqrt{2}$$

$$b) \frac{\sqrt{180}}{\sqrt{20}} = 3$$

Gib die Definitionsmenge an und berechne:

$$c) \frac{\sqrt{63xy^3} \cdot \sqrt{56x^2y}}{\sqrt{7y} \cdot \sqrt{21xy}} = 2\sqrt{6} \cdot \sqrt{\frac{x^3y^4}{xy^2}} = 2\sqrt{6} \cdot \sqrt{x^2y^2} = 2\sqrt{6}xy$$

$$x, y \neq 0, x > 0; y > 0$$

$$d) \frac{\sqrt{48a^4bc^3}}{\sqrt{3b^3c^5}} = 4 \cdot \sqrt{\frac{a^4}{b^2c^2}} = 4 \frac{a^2}{bc}$$

$$b, c \neq 0 \text{ und } b > 0; c > 0$$

Mache den Nenner rational:

$$e) \frac{3\sqrt{5}}{2\sqrt{5}-5} = -3\sqrt{5} - 6$$

$$f) \frac{4-\sqrt{3}}{4+\sqrt{3}} = \frac{(4-\sqrt{3}) \cdot (4-\sqrt{3})}{(4+\sqrt{3}) \cdot (4-\sqrt{3})} = \frac{19-8\sqrt{3}}{13}$$

Fasse zusammen:

$$g) 4 \cdot \sqrt{y+3} - \frac{3y}{\sqrt{y+3}} = \frac{4 \cdot \sqrt{y+3} \cdot \sqrt{y+3}}{\sqrt{y+3}} - \frac{3y}{\sqrt{y+3}} = \frac{4 \cdot (y+3) - 3y}{\sqrt{y+3}} = \frac{4y+12-3y}{\sqrt{y+3}} = \frac{y+12}{\sqrt{y+3}}$$